

① Factor

① (a) $2x^2 + 14x + 20$

① (b) $6x^2 + 2x - 8$

② Given the vertex $(-1, 4)$ and another point, $(1, -4)$
find the polynomial, vertex, and factored forms of
the quadratic.

③ Sketch w/o a calculator $f(x) = \frac{1}{3}(x+1)(x-2)^2$

① Factor

$$\textcircled{a} \quad 2x^2 + 14x + 20$$

1 · 2	2 · 7	1 · 20
	1 · 14	2 · 10
		<u>4 · 5</u>

$$(2x + 4)(x + 5)$$

$$(x + 2)(2x + 10)$$

$$\textcircled{b} \quad 6x^2 + 2x - 8$$

1 · 6	1 · 2	1 · 8
2 · 3		<u>-2 · 4</u>
		1 · -8
		2 · -4

$$(3x + 4)(2x - 2) \checkmark$$

$$(6x + 8)(x - 1)$$

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F
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$$2x^2 + 14x + 20$$

① Mult $a \cdot c$

$$2 \cdot 20 = 40$$

$$1 \cdot 40$$

$$2 \cdot 20$$

$$8 \cdot 5$$

$$4 \cdot 10$$

② Add to b -term

$$4, 10$$

$$\textcircled{3} \quad 2x^2 + 4x \left\{ 10x + 20 \right.$$

④ Pull out the common factors

$$2x(x+2) + 10(x+2)$$

$$(x+2)(2x+10)$$

② Given the vertex $(-1, 4)$ and another point, $(1, -4)$
find the polynomial, vertex, and factored forms of the quadratic.

$$y = a(x-h)^2 + k$$

$$y = a(x+1)^2 + 4$$

$$-4 = a(1+1)^2 + 4$$

$$\begin{array}{rcl} -4 & = & 4a + 4 \\ -4 & & -4 \end{array}$$

$$\begin{array}{rcl} -8 & = & 4a \\ \frac{-8}{4} & & \frac{4}{4} \end{array} \quad a = -2$$

$$y = -2(x+1)^2 + 4$$

$$\begin{aligned} y &= -2(x+1)(x+1) + 4 \\ &= -2(x^2 + 2x + 1) + 4 \end{aligned}$$

$$-2x^2 - 4x - 2 + 4$$

$$-2x^2 - 4x + 2$$

$$y = -2(x+1)^2 + 4$$

$$\begin{array}{rcl} 0 & = & -2(x+1)^2 + 4 \\ -4 & & -4 \end{array}$$

$$\begin{array}{rcl} -4 & = & -2(x+1)^2 \\ \frac{-4}{-2} & & \frac{-2}{-2} \end{array}$$

$$\sqrt{2} = \sqrt{(x+1)^2}$$

$$\pm\sqrt{2} = x+1$$

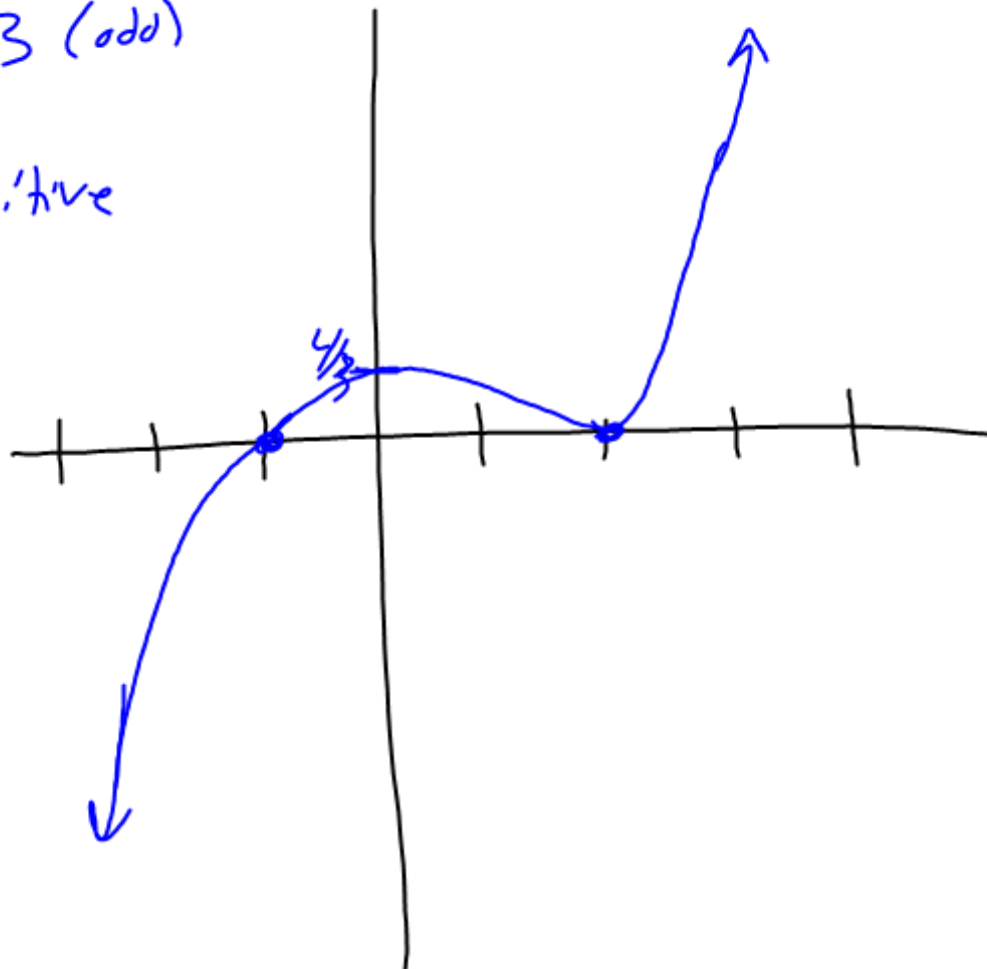
$$x = \pm\sqrt{2} - 1$$

$$y = a(x-R_1)(x-R_2)$$

$$y = -2(x - (\sqrt{2}-1))(x - (-\sqrt{2}-1))$$

degree: 3 (odd)

L.C. positive



(32)

$$x^4 - x^3 - 20x^2$$

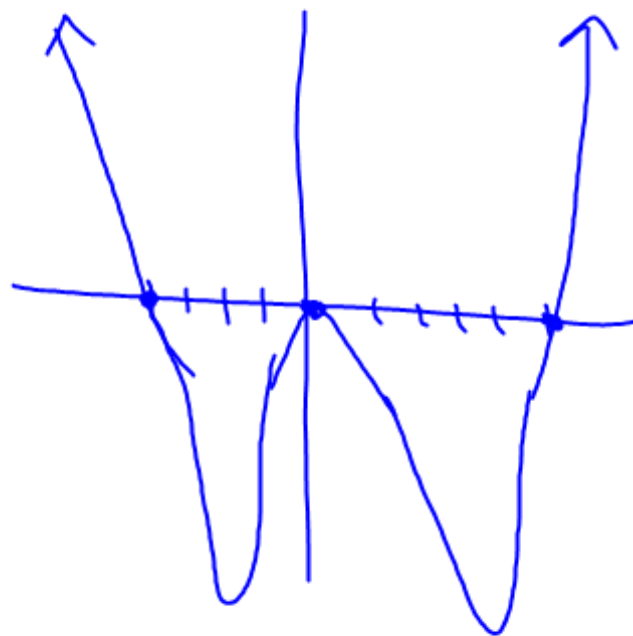
$$0 = x^2(x^2 - x - 20)$$

$$x^2(x-5)(x+4) \rightarrow (x)(x)(x-5)(x+4)$$

$$\begin{array}{ccc} \downarrow & \downarrow & \downarrow \end{array}$$

$$0, 0 \quad 5 \quad -4$$

degree 4



(35)

$$3x^2 - 12x + 3$$

$$x = \frac{12 \pm \sqrt{144 - 4(3)(3)}}{6}$$

$$\begin{aligned} x &= \frac{12 \pm \sqrt{108}}{6} \Rightarrow \frac{12 \pm \sqrt{27} \cdot \sqrt{4}}{6} = \frac{12 \pm \sqrt{9} \cdot \sqrt{3} \cdot \sqrt{4}}{6} \\ &= \frac{12 \pm 6\sqrt{3}}{6} = \boxed{2 \pm \sqrt{3}} \end{aligned}$$

Factor

$$\begin{array}{l}
 x^4 - x^2 - 6 \\
 x^2 - x - 6 \\
 \rightarrow (x^2 - 3)(x^2 + 2)
 \end{array}$$

$$x^8 - x^4 - 6$$

$$(\quad)(\quad)$$

$$\begin{array}{l}
 0 = \frac{1}{4} (x)^3 (x^2 - 9) \\
 \downarrow \\
 0 (x - 3)(x + 3) \\
 \downarrow \quad \downarrow \\
 3 \quad -3
 \end{array}$$

Sect. 2.2

#39, 40, 42, 45, 49, 53-60(2), 61-72(2)